

# **Application of Design of Experiments in Cost Estimating**

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# Outline

- ◆ Purpose
- ◆ Problem Statement
- ◆ Objective
- ◆ Application
- ◆ Design Of Experiments Overview
- ◆ Case Study
- ◆ Conclusion
- ◆ Acknowledgments

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# Purpose

- ◆ Create an awareness of Design of Experiments as another tool for the cost community

# Problem Statement

- ◆ Background
  - Sheet count method to determine engineering efforts
  - Wide variance between bid and actual
- ◆ Supporting Data
  - Design labor hour estimates are low (on the average).
  - The standard deviation of bids ranged from 30-40%. This was the value that the project was being managed.
  - Across the product lines (7) in our division, the hours/sheet (and hours/ft<sup>2</sup>) were a factor of 4 from largest to smallest.
    - Complexity is too variable to standardize process across product lines
- ◆ In addition to the above challenges, we still had to estimate sheets which is neither supportable nor a consistent process.

# Objective

- ◆ Develop quick, accurate and reliable cost estimates
  - Simple process
  - Low level of training
  - Consistency
  - Audit trail
- ◆ This process will be used by:
  - Project Managers
    - For quick response during proposal efforts
  - Engineers
    - For making design decisions

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# Application

- ◆ Establish a parametric cost estimating model for budgetary mechanical engineering estimating hours using DOE.

# Design Of Experiments Overview

- ◆ Design Of Experiments (DOE) Definition
- ◆ DOE Process
- ◆ DOE Tools / Approaches
- ◆ DOE Tool Comparison
- ◆ Example Full Factorial Matrix
- ◆ DOE Statistical Analysis Overview

# DOE Definition

- ◆ DOE organizes the collection of data to determine the most statistically confident relationship between inputs and outputs.
  - Complexity of the relationship is chosen by the user.
- ◆ Key terms
  - Variables, inputs, key cost drivers, factors
  - Response, output, results
  - Levels, settings, conditions, limits
  - Equation, relationship, algorithm
  - One Factor at a Time (OFAT)



# DOE Process

- ◆ Define goal - need
- ◆ Define response(s) to measure progress to goal
- ◆ List all variables and down select to “key” variables using experience
- ◆ Select appropriate design matrix - approach
- ◆ Select levels for variables
- ◆ Address tradeoffs between responses
- ◆ Perform test - simulation
- ◆ Analyze results
- ◆ Discuss next step

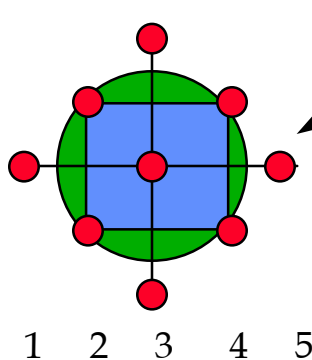
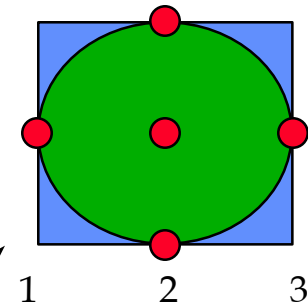
# DOE Tools / Approaches

◆ Factorial Designs

- Full ( $2^k$  form)
- Fractional ( $2^{k-p}$  form)
- Taguchi - maximum assumptions

◆ Advanced Designs (Response Surface Methods)

- 3 level (not a  $3^k$  form)
  - Box-Behnken, predictable to limits
- 5 level (composite with factorial as a basis)
  - Central Composite Design (CCD), predictable in only a portion of limits
- Optimization
  - Numerical
  - Graphical



Organizing the collection of data to determine the most statistically confident relationship

# DOE Tool Comparison

OFAT or Taguchi typical output equation (main effects)

$$y = z + a*A + b*B + c*C$$

More information  
(fine tuning) is  
achieved as  
progress to more  
rigorous tools

Factorial typical output equation (main and interactions)

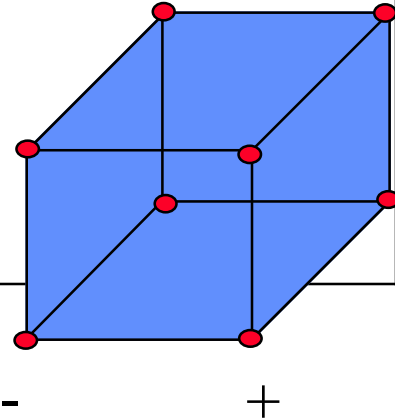
$$y = z + a*A + b*B + c*C + d*A*B + e*A*C + f*B*C + g*A*B*C$$

Response Surface typical output equation (main, interactions, quadratic)

$$y = z + a*A + b*B + c*C + d[A]^2 + e[B]^2 + f[C]^2 + g[AB] + h[AC] + \\ i[BC] + j[ABC] + p[A]^3 + q[B]^3 + r[C]^3 + s[A^2B] + t[AB^2] + u[A^2C] \\ + v[AC^2] + w[B^2C] + x[BC^2]$$

# Example Full Factorial Matrix

Test #	Variable			Output			
	A	B	C	1	2	3	4
1	-	-	-				
2	+	-	-				
3	-	+	-				
4	+	+	-				
5	-	-	+				
6	+	-	+				
7	-	+	+				
8	+	+	+				



Predetermined, organized combinations to provide resultant equation with reasonably expected terms - 3 variables at 2 levels: 8 total tests ( $2^3$ )

# DOE Statistical Analysis Overview

- ◆ Purpose is for the user to determine a statistically valid equation for the output
  - F-Test on model
  - $R^2$  curve fit assessment
  - Prob  $> |t|$  for all variable terms
  - t value (outlier t) of test runs
  - Residual Analysis

If these are acceptable to the user, the final equation is valid for predictive usage.

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# Case Study

- ◆ Project Goal
- ◆ Response (Output)
- ◆ DOE Process Steps
- ◆ Cost Driver Identification
- ◆ Manufacturing Complexity Case
- ◆ Labor Hour Case
- ◆ Next Step
- ◆ Validation Results
- ◆ Result Comparison

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# Project Goal

- ◆ Perform accurate, consistent and reliable budgetary cost estimating hours in mechanical engineering department
- ◆ Utilize DOE as a tool to assist in this process

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# Response (Output)

- ◆ Mechanical engineering labor hours consists of:
  - Layout and design
  - Analysis
  - Detailing
  - Data package



# DOE Process Steps

- ◆ Identify cost drivers
- ◆ Select appropriate DOE matrix for two cases
  - Case 1. manufacturing complexity
  - Case 2. labor sensitivity analysis
- ◆ Collect historic data and identify limits for key cost drivers
- ◆ Run the PRICE H model for the established test combinations to obtain the output
- ◆ Perform statistical analysis on DOE software

Assumes a calibrated  
PRICE H model

# Cost Driver Identification

- ◆ Labor hours
  - Weight, manufacturing complexity, % of new design, design repeat, platform (level of specification), design effort, and engineering experience
  - Manufacturing complexity
  - # of parts, precision, assembly difficulty, process and material type, and platform
- ◆ This led to a two-tiered DOE approach
  - One DOE matrix for manufacturing complexity
  - One DOE matrix for labor hours

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# Manufacturing Complexity Case

- ◆ Manufacturing Complexity DOE
- ◆ Assembly Difficulty
- ◆ Manufacturing Complexity Chart

# Manufacturing Complexity DOE

Cost Driver      Low      Most Likely      High

# of parts	10	45	80
precision	.001	.050	.100
assembly difficulty*	A	B	C
machine / material	titanium	steel	aluminum
platform	com. ground	military ground	air / ground

Incorporate into CCD tool. Has 27 combinations versus the 3125 possible (5<sup>5</sup>).

\* defined on next page

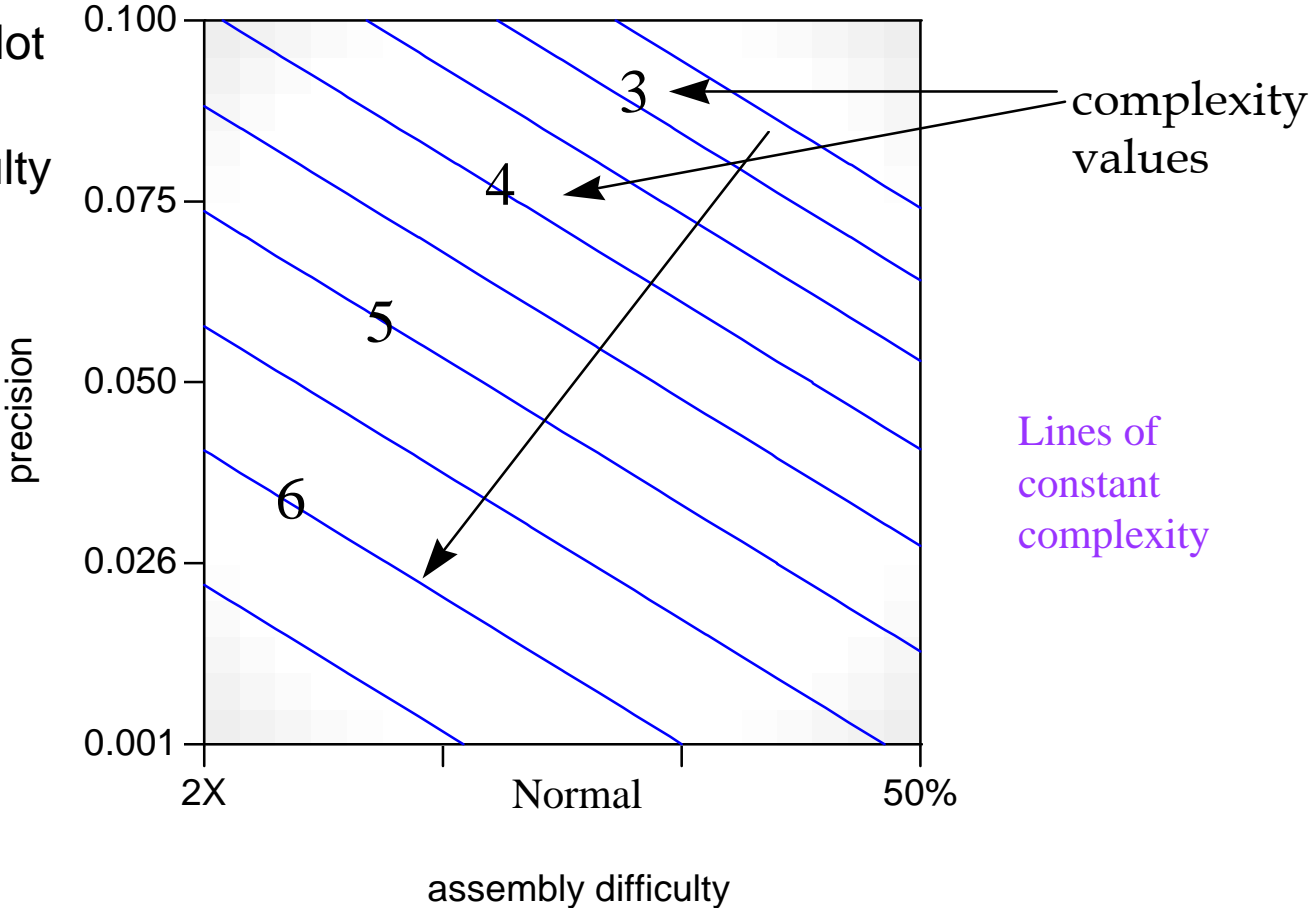
*Precision and assembly difficulty dominate. These replace the complexity term in the labor equation if complexity is significant.*

# Assembly Difficulty

- ◆ A: Assembly tolerance 2 times tougher than part tolerance
- ◆ B: Assembly tolerance same as part tolerance, most commonly used
- ◆ C: Assembly tolerance 50% less than part tolerance
  - As defined in PRICE-H

# Manufacturing Complexity Chart

DESIGN EXPERT Plot  
Actual Factors:  
X = assembly difficulty  
Y = precision



Proprietary data removed.

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# Labor Hour Case

- ◆ Labor Hour DOE
- ◆ Design Effort
- ◆ Labor Hour DOE Findings
- ◆ Response Surface of Labor Hours

# Labor Hour DOE

Cost Driver    Low            Most Likely            High

weight	50	525	1000
mfg cplx	4	5	6
% new des	10%	45%	80%
design rep	0%	45%	90%
platform	1.0	1.3	1.6
design effort*	A	B	C
eng exp	extensive	normal	many new

Incorporate into Box-Behnken tool. Has 57 combinations versus 2187 possible (3<sup>7</sup>).

\* defined on next page

*All important - quadratic terms and interactions exist*



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# Design Effort

- ◆ A - extensive mod to existing design
- ◆ B - new design within established product line: existing state of the art
- ◆ C - new design different from established product line: must develop new technology or material
  - As defined in PRICE-H

# Labor Hour DOE Findings

- ◆ All variables (cost drivers) are statistically significant
- ◆ Labor Hours =  $f(\text{Weight}^2, \text{New design}^2, \text{Design effort}^2)$
- ◆ Weight interacts (has synergy) with
  - All cost drivers except engineering experience
- ◆ Manufacturing complexity interacts (has synergy) with
  - New design, design repeat, platform and design effort
- ◆ New design interacts (has synergy) with
  - Design repeat, platform and design effort

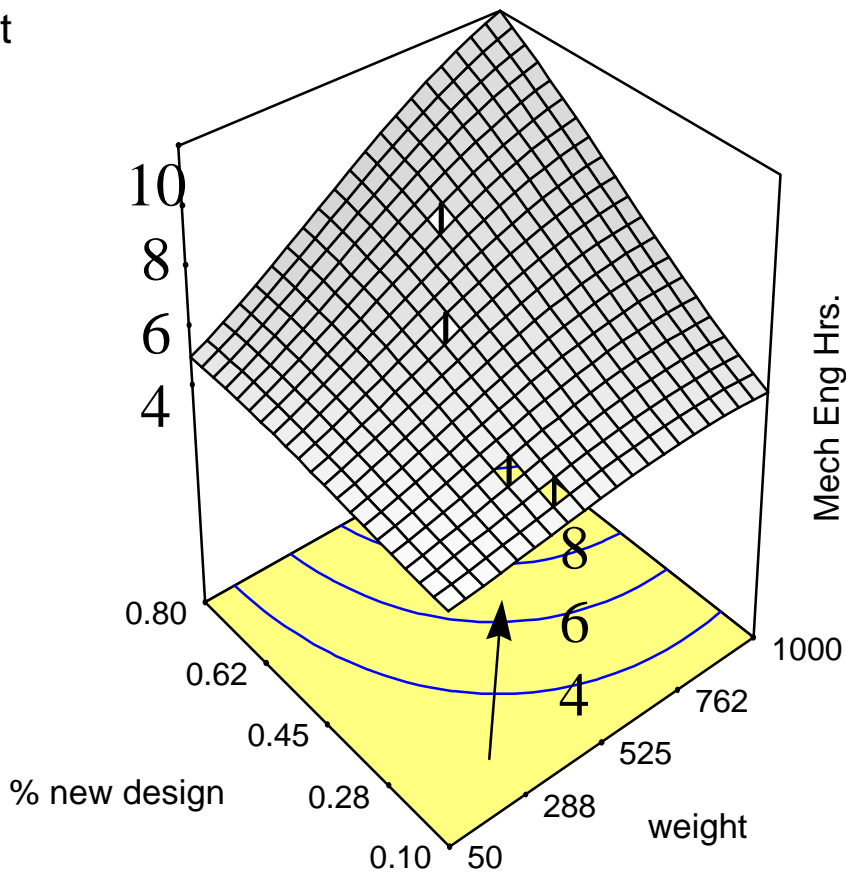
Together these items create  
the final equation for hours.

# Response Surface of Labor Hours

DESIGN EXPERT Plot

Actual Factors:  
X = weight  
Y = % new design

Actual Constants:  
mfg cmplx = 5.0  
design repeat = 0.45  
platform = 1.3  
design eff = 3.5  
eng exper = 0



3D and  
2D view  
shown  
on same  
chart

Proprietary data  
removed.

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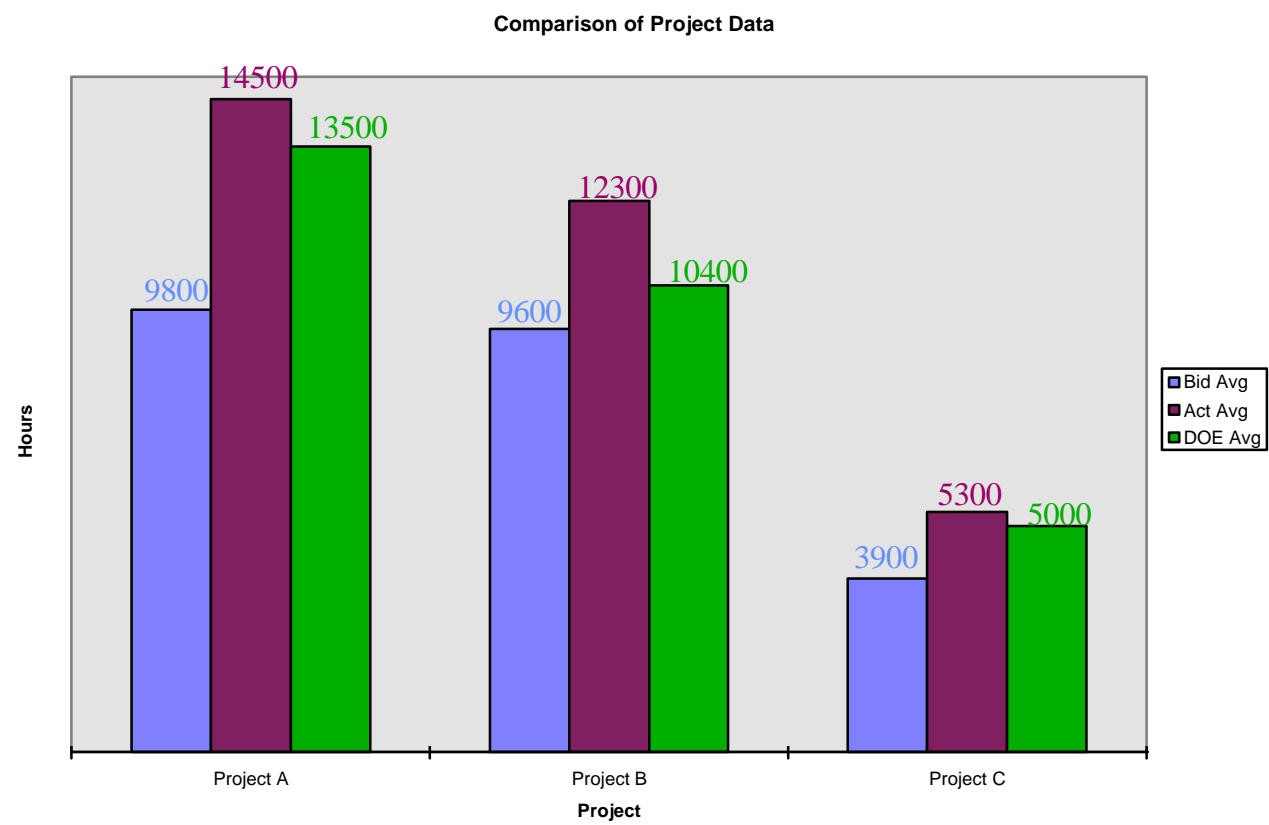
# Next Step

- ◆ The final equations are statistically valid.
- ◆ Create instructions to clearly define the process
- ◆ Validate DOE model with actual project data
  - Compare with PRICE H as a sanity check

# Validation Results

- ◆ The DOE model followed the PRICE H runs (design and drafting hours) within a reasonable percentage (roughly 4%)
- ◆ Thus far, the DOE model follows the actual data rather well. When combining several estimates together, the comparison to actual was very close (within 7%).
- ◆ The standard deviation for the DOE model versus actuals is similar to the sheet count method.
- ◆ The validation effort is still in process.

# Result Comparison



Project B has very small sample size

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# Conclusion

- ◆ Initial results show methodology works well after comparing to actuals from a few projects
- ◆ Will be folded into a larger mechanical engineering cost estimating process
- ◆ DOE analysis will be repeated periodically. This will update for the full PRICE H model calibrations.
- ◆ DOE is an applicable tool and is available for use.

# Acknowledgments

- ◆ PRICE-H user manual
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